

Part 2. Charm quark in quark matter

Content of Part 2

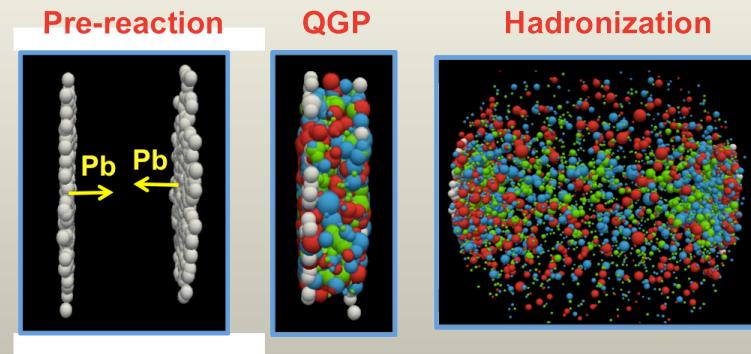
1. Heavy quark in quark matter
2. “Kondo phase” of heavy quark matter
S.Y., K. Suzuki, K. Itakura, arXiv:1604.09229 [hep-ph]
3. Case of single heavy quark
S.Y., arXiv:1608.06450 [hep-ph]

1. Heavy quark in quark matter

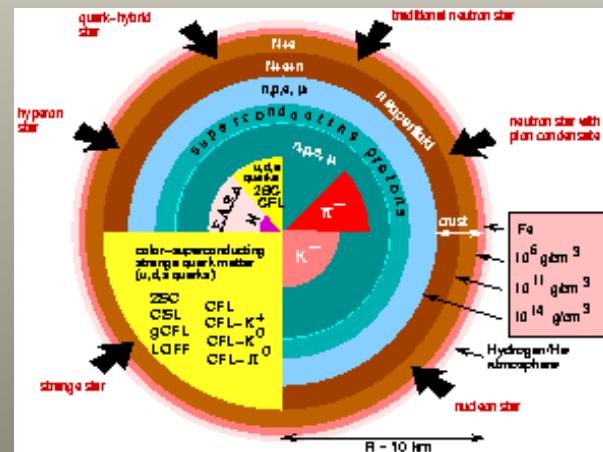
Charm quark in quark matter

Do charm/bottom quarks exist in quark matter?

① Charm quark production at initial (gluon) hard scatterings in relativistic heavy ion collisions (ex. J-PARC).



② Flavor change (ex. $s \rightarrow c$) by high energy neutrinos in strange quark matter in neutron stars.



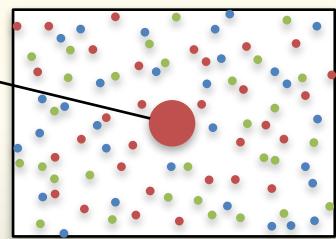
2. “Kondo phase” of heavy quark matter

Lagrangian

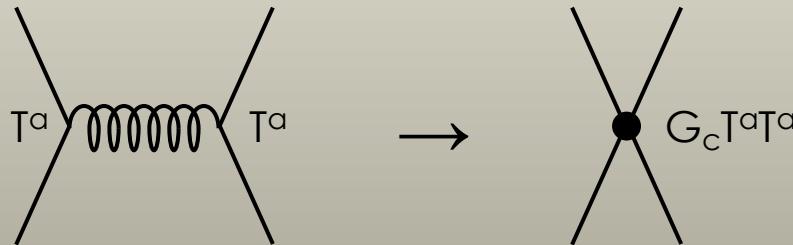
Light quark (u,d,s) ψ and heavy quark (c) Ψ

$$\mathcal{L} = \bar{\psi} i \not{D} \psi + \mu \bar{\psi} \gamma^0 \psi + \bar{\Psi} i \not{D} \Psi - m_Q \bar{\Psi} \Psi - G_c \sum_a (\bar{\psi} \gamma^\mu T^a \psi) (\bar{\Psi} \gamma_\mu T^a \Psi) ,$$

Cf. NJL for light quark
 $G_c = (9/2) 2.0 / \Lambda^2$
 $\Lambda = 0.65$ [GeV]



① Color-current interaction



Cf. S.Y., K. Sudoh, PRC88, 015201 (2013)
K. Hattori, K. Itakura, S. Ozaki, S.Y., PRD92, 065003 (2015)

② N_f flavor for light quark

$$\psi = (\psi^1, \dots, \psi^{N_f})^t$$

③ Heavy quark limit for charm quark $p^\mu = m_Q v^\mu + k^\mu$ $v^\mu v_\mu = 1$

$$\Psi \rightarrow \Psi_v = \frac{1}{2}(1 + \not{v}) e^{im_Q v \cdot x} \Psi$$

← Heavy Quark Effective Theory
Cf. “Heavy Quark Physics”,
V. A. Manohar and M. B. Wise

2. “Kondo phase” of heavy quark matter

Mean-field approximation

S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]

① Mean-field: mixing between light quark and heavy quark

$$(\bar{\psi}_\alpha^i \Psi_{v\delta})(\bar{\Psi}_{v\gamma} \psi_\beta^i) \rightarrow \langle \bar{\psi}_\alpha^i \Psi_{v\delta} \rangle \bar{\Psi}_{v\gamma} \psi_\beta^i + \langle \bar{\Psi}_{v\gamma} \psi_\beta^i \rangle \bar{\psi}_\alpha^i \Psi_{v\delta} \\ - \langle \bar{\psi}_\alpha^i \Psi_{v\delta} \rangle \langle \bar{\Psi}_{v\gamma} \psi_\beta^i \rangle \quad \text{i=light flavor; } \alpha, \beta, \gamma, \delta = \text{Dirac indices}$$



② Gap (color singlet)

$$\Delta_{\delta\alpha}^i \equiv \frac{G_c}{2} \langle \bar{\psi}_\alpha^i \Psi_{v\delta} \rangle \rightarrow \Delta_{\delta\alpha}^i = \Delta^i \left(\frac{1+\gamma_0}{2} (1 - \hat{k} \cdot \vec{\gamma}) \right)_{\delta\alpha}$$



③ Mean-field Lagrangian

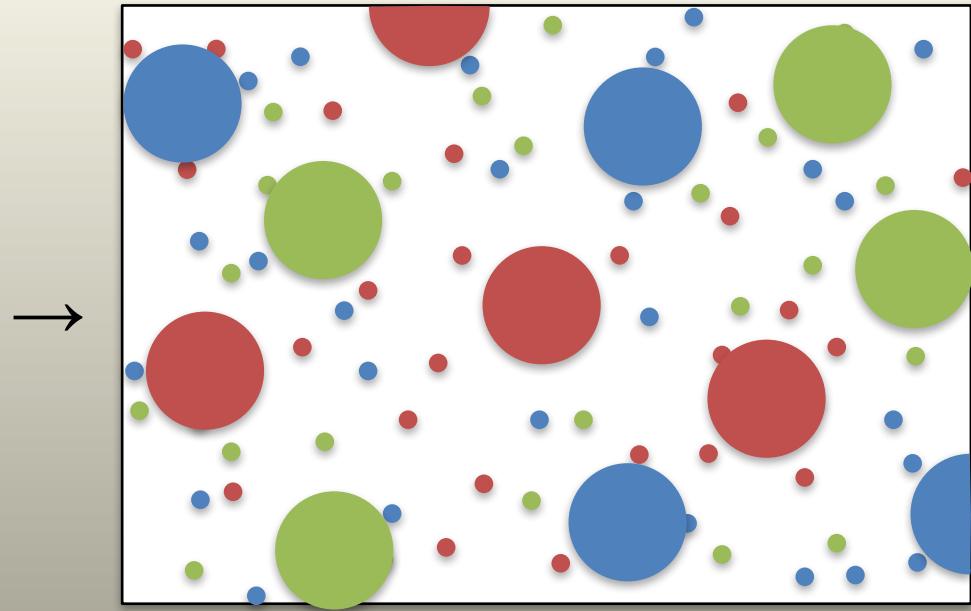
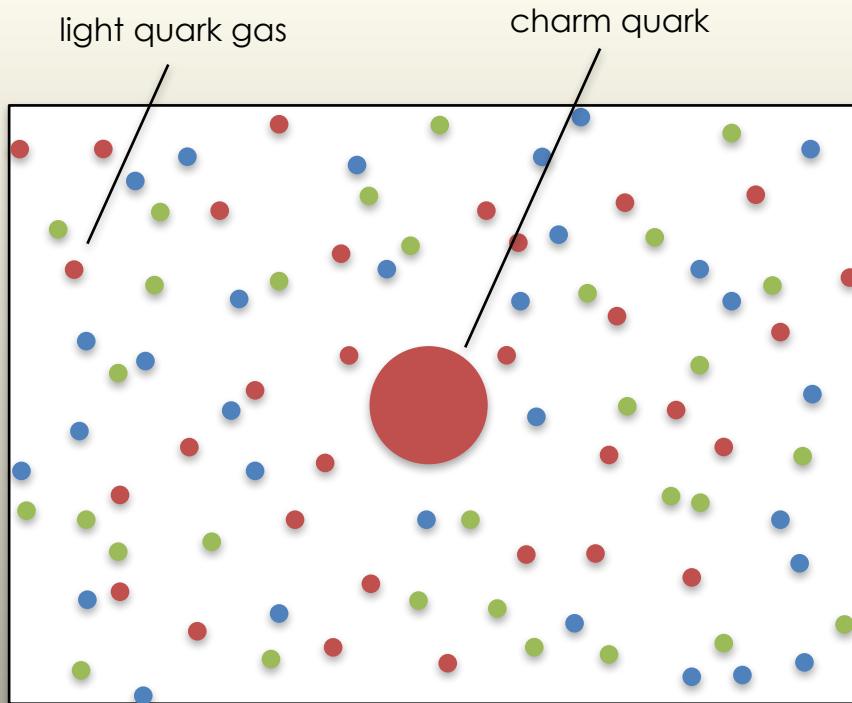
Lagrange multiplier for heavy quark density n_Q

$$\mathcal{L}^{\text{MF}} = \bar{\psi} (\not{k} + \mu \gamma^0) \psi + \bar{\Psi}_v v \cdot k \Psi_v - \lambda (\Psi_v^\dagger \Psi_v - n_Q) \\ + \sum_i \Delta^i \bar{\Psi}_v \frac{1 + \gamma_0}{2} \left(1 + \hat{k} \cdot \vec{\gamma} \right) \psi^i \\ + \sum_i \Delta^{i*} \bar{\psi}^i \left(1 + \hat{k} \cdot \vec{\gamma} \right) \frac{1 + \gamma_0}{2} \Psi_v - \sum_i \frac{8}{G_c} |\Delta^i|^2$$

2. “Kondo phase” of heavy quark matter

Charm quark density $n_Q(\lambda)$

S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]



Breaking of translational invariance...

S.Y., arXiv:1608.06450 [hep-ph]

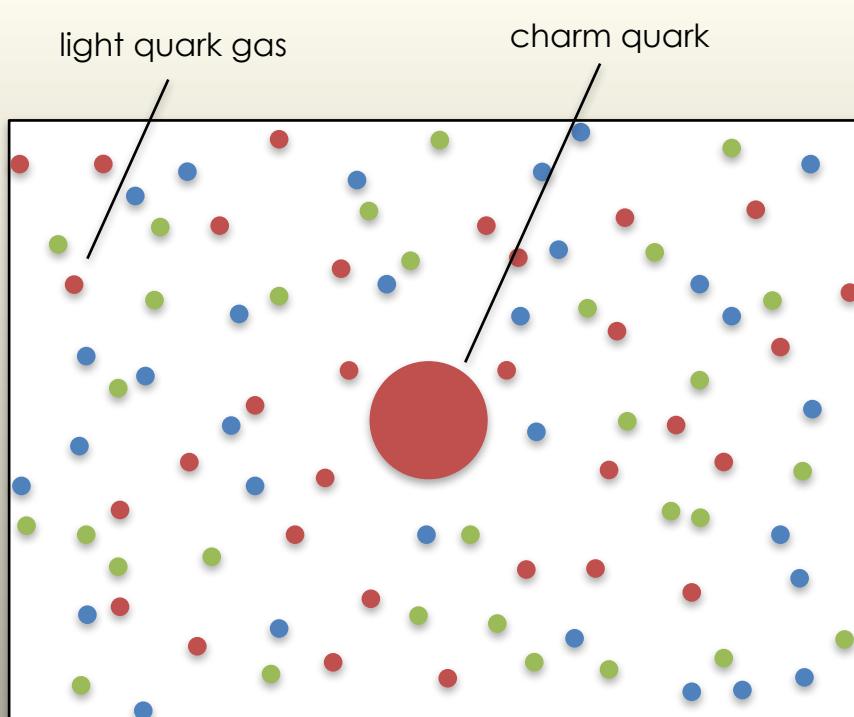
Conservation of translational invariance!

$$\Psi_v^\dagger(x)\Psi_v(x) = \sum_i \delta^{(3)}(\vec{x} - \vec{x}_i)$$

2. “Kondo phase” of heavy quark matter

Charm quark density $n_Q(\lambda)$

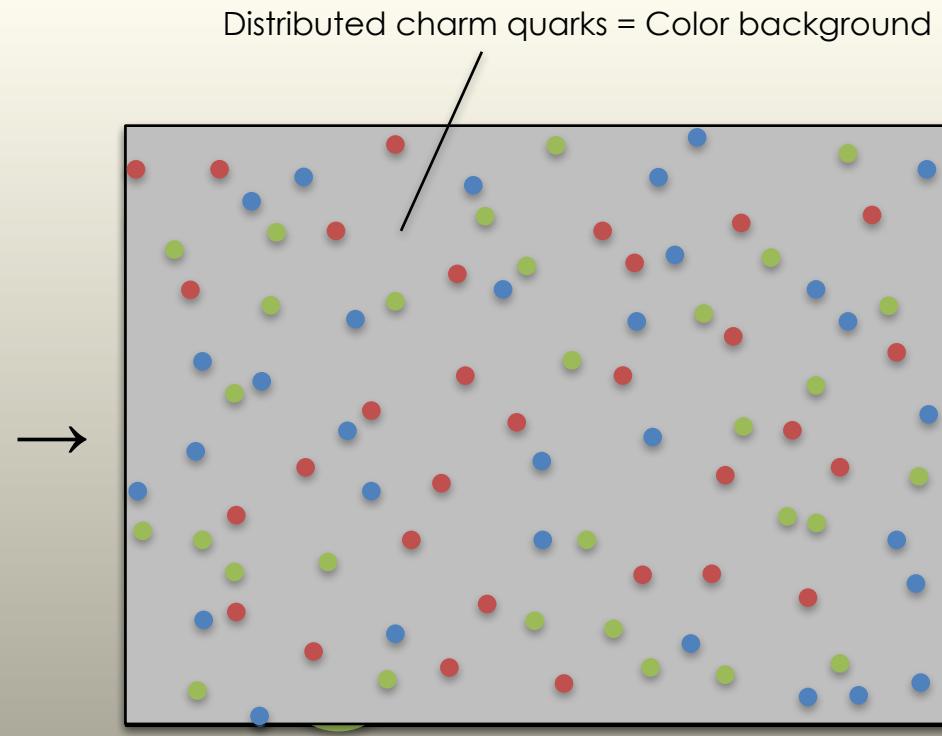
S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]



single charm quark

Breaking of translational invariance...

S.Y., arXiv:1608.06450 [hep-ph]



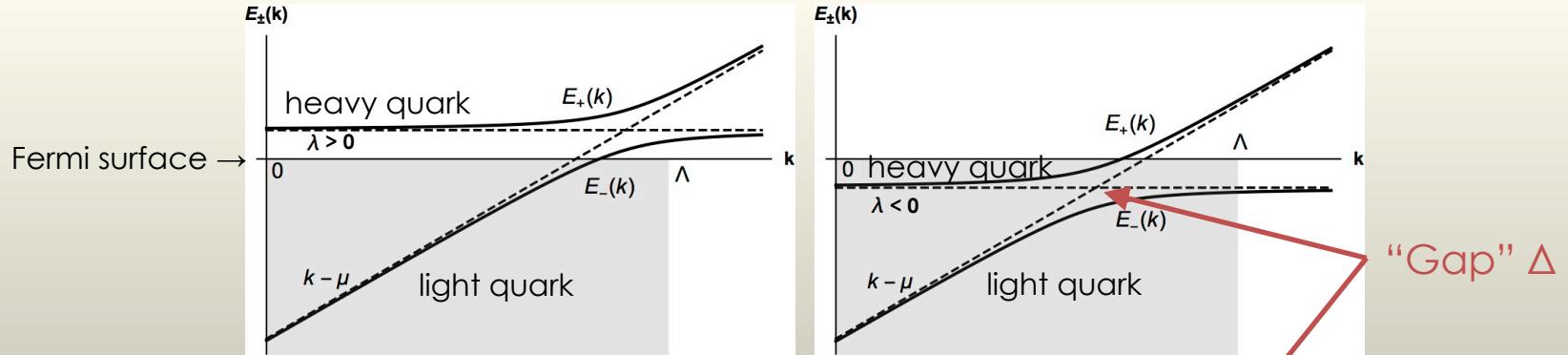
many charm quarks distributed randomly
(No Fermi surface)

Conservation of translational invariance!

$$\Psi_v^\dagger(x)\Psi_v(x) = \sum_i \delta^{(3)}(\vec{x} - \vec{x}_i)$$
$$\rightarrow n_Q \equiv \overline{\sum_i} \delta^{(3)}(\vec{x} - \vec{x}_i)$$

2. “Kondo phase” of heavy quark matter

Energy-momentum dispersion & thermodynamic potential



“mixing” mode $E_{\pm}(k) \equiv \frac{1}{2} \left(k + \lambda - \mu \pm \sqrt{(k - \lambda - \mu)^2 + 8N_f |\Delta|^2} \right), \quad k = |\vec{k}|$

“free” mode
$$\begin{cases} E(k) \equiv E_i = k - \mu & [i = 1, \dots, N_f - 1], \\ \tilde{E}(k) \equiv \tilde{E}_i = -k - \mu & [i = 1, \dots, N_f], \end{cases} \quad \Delta^i = \Delta$$

Thanks to Kanazawa-san's comments.

$$\Omega(T, \mu, \lambda; \Delta) = 2N_c \int_0^\Lambda f(T, \mu, \lambda; k) \frac{k^2 dk}{2\pi^2} + \frac{8N_f}{G_c} |\Delta|^2 - \lambda n_Q$$

$$f(T, \mu, \lambda; k) \equiv -\beta^{-1} \ln[(1 + e^{-\beta E_+(k)})(1 + e^{-\beta E_-(k)})(1 + e^{-\beta E(k)})^{N_f - 1}]$$

$$\textcircled{1} \quad \frac{\partial}{\partial \Delta^*} \Omega(T, \mu, \lambda; \Delta) = 0 \quad \textcircled{2} \quad -\frac{\partial}{\partial \mu} \Omega(T, \mu, \lambda; \Delta) = n_q \quad \textcircled{3} \quad \frac{\partial}{\partial \lambda} \Omega(T, \mu, \lambda; \Delta) = 0$$

2. “Kondo phase” of heavy quark matter

Gap equation @ $\lambda=0$

S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]

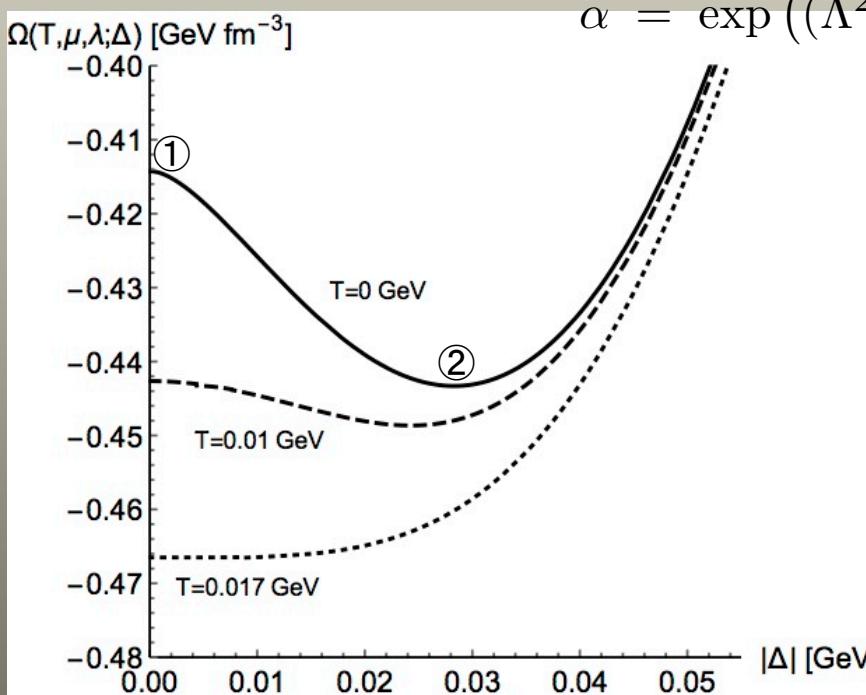
$$\Delta = \frac{1}{2} N_c G_c \int_0^\Lambda \frac{\Delta}{\sqrt{(k - \mu)^2 + 8N_f|\Delta|^2}} \frac{k^2 dk}{2\pi^2} \quad @\lambda=0, T=0$$

↓

① trivial solution ② non-trivial solution

$$|\Delta| = 0 \quad |\Delta| \simeq \alpha \sqrt{\frac{\mu(\Lambda - \mu)}{2N_f}} \exp\left(-\frac{2\pi^2}{N_c \mu^2 G_c}\right)$$

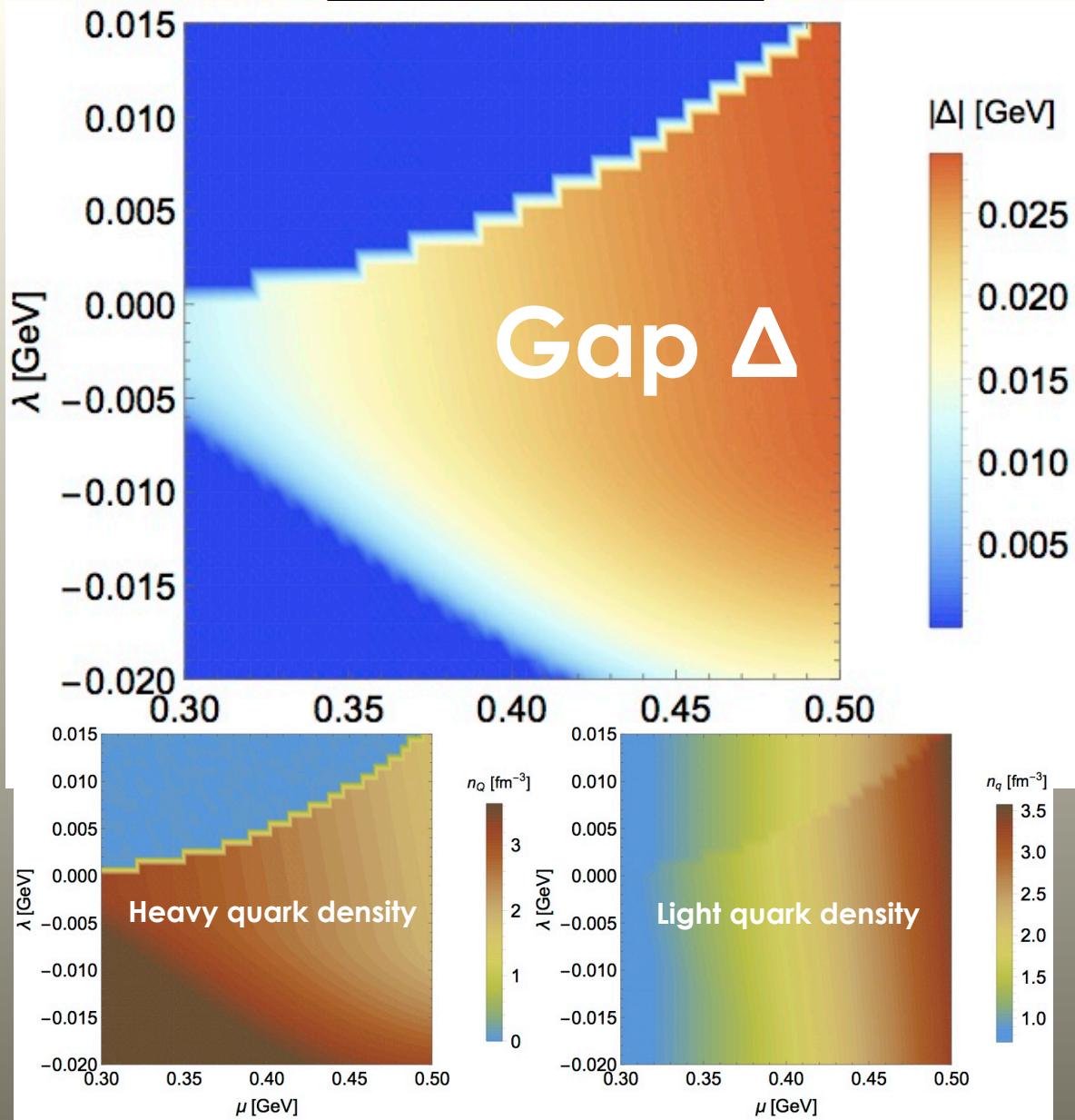
$$\alpha = \exp\left((\Lambda^2 + 2\Lambda\mu - 6\mu^2)/4\mu^2\right)$$



2. “Kondo phase” of heavy quark matter

“Kondo phase” @T=0

S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]

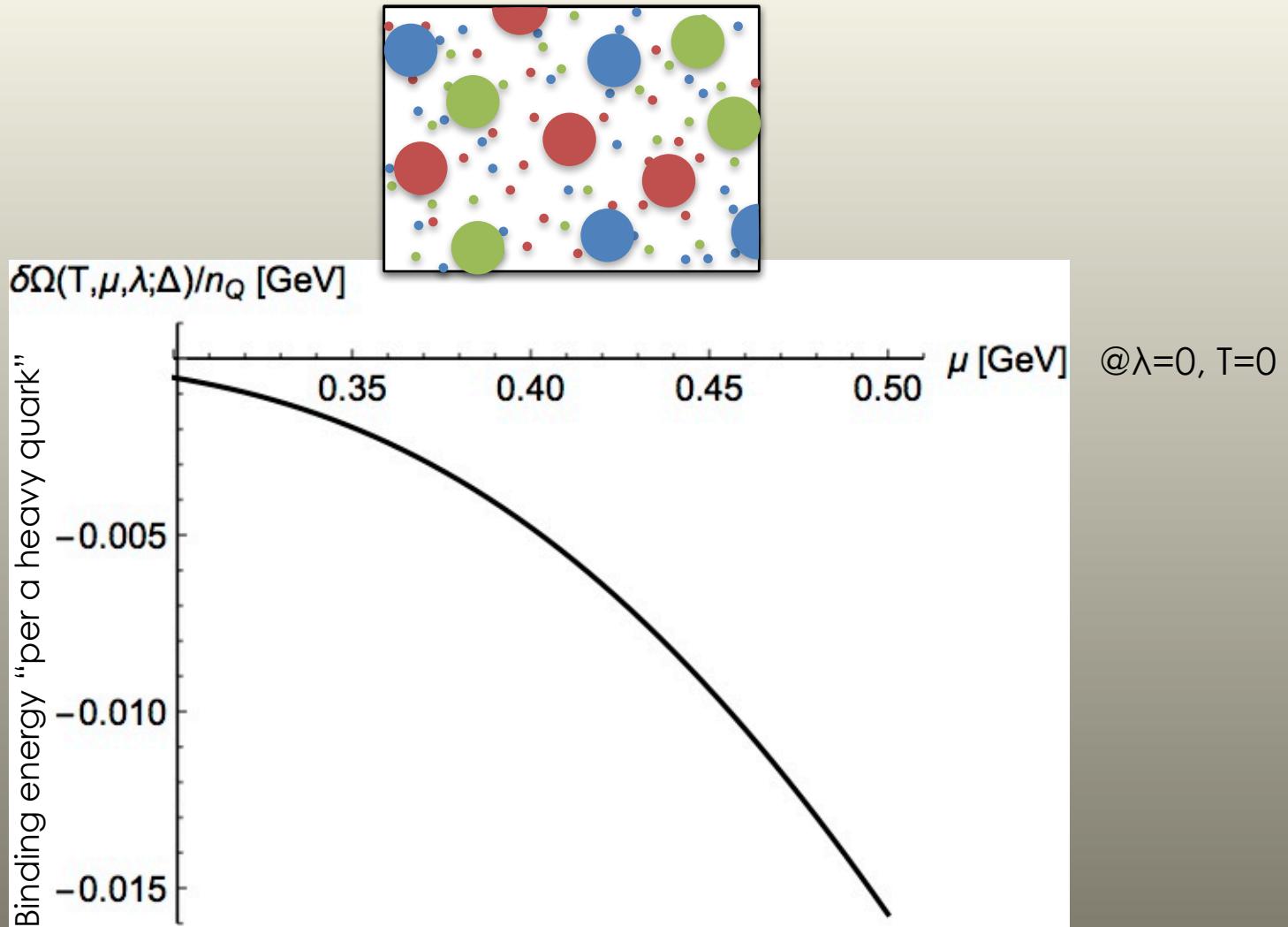


2. “Kondo phase” of heavy quark matter

Energy-gain “per a heavy quark”

S.Y., K. Suzuki, K. Itakura,
arXiv:1604.09229 [hep-ph]

$$\delta\Omega(T, \mu, \lambda; \Delta)/n_Q \text{ with } \delta\Omega(T, \mu, \lambda; \Delta) = \Omega(T, \mu, \lambda; \Delta) - \Omega(T, \mu, \lambda; 0)$$



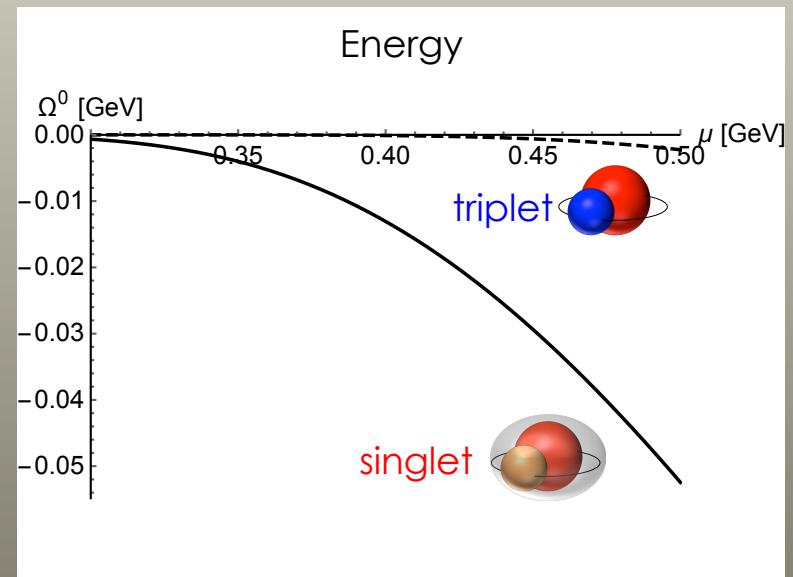
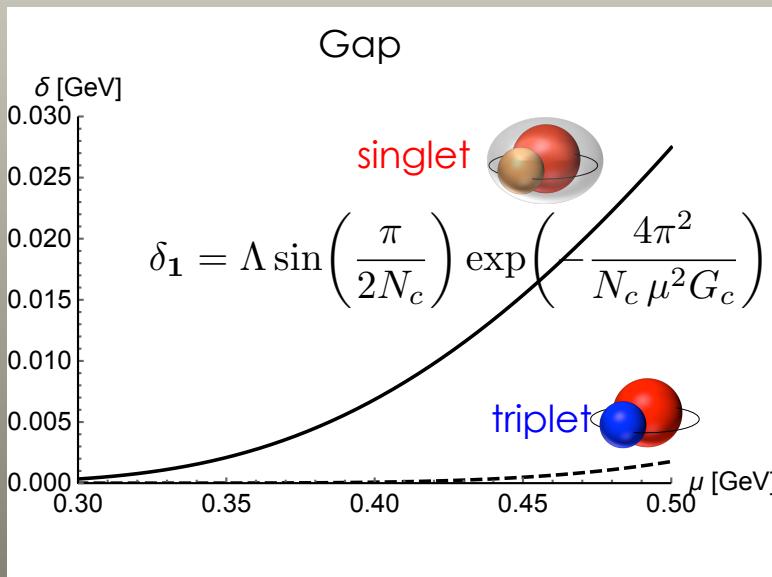
3. Case of single heavy quark

Energy-gain of a heavy quark

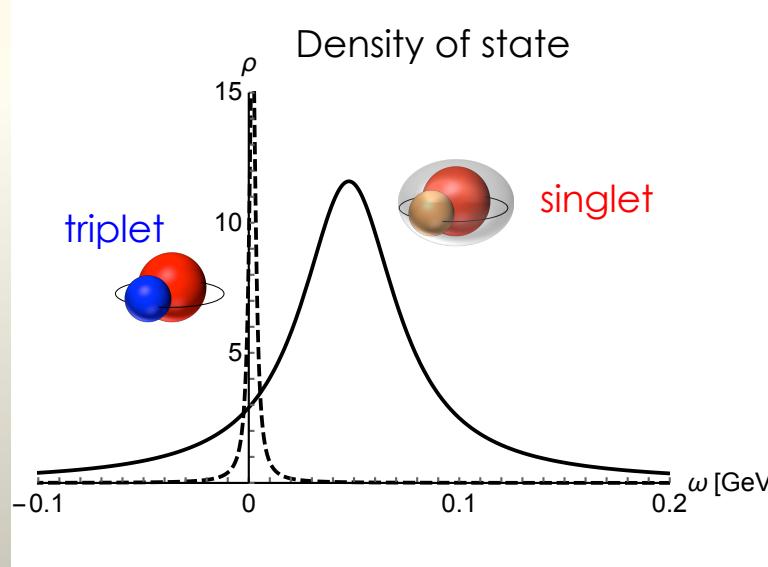
S.Y., arXiv:1608.06450 [hep-ph]

$$\text{Energy: } \Omega_1(\lambda, \Delta_1) = -\frac{1}{\beta} \int_{-\infty}^{+\infty} \ln(1 + e^{-\beta\omega}) 2N_c \rho_1(\omega) d\omega + \frac{8N_f |\Delta_1|^2}{G_c} V - \lambda$$

$$\begin{aligned} \text{Density of state: } \rho_1(\omega) &= -\frac{1}{\pi} \text{Im} \frac{\partial}{\partial \omega} \ln \left(\omega_+ - \lambda - \sum_{\vec{q}} \frac{2N_f |\Delta_1|^2}{\omega_+ + \mu - q} \right) \\ &= \frac{1}{\pi} \frac{\delta_1}{(\omega - \lambda_1)^2 + \delta_1^2} \\ &\quad \sum_{\vec{q}} \frac{2N_f |\Delta_1|^2}{\omega_+ + \mu - q} \simeq -\frac{iN_f}{\pi} \mu^2 |\Delta_1|^2 V \equiv -i\delta_1 \\ &\quad \text{(approximation)} \end{aligned}$$

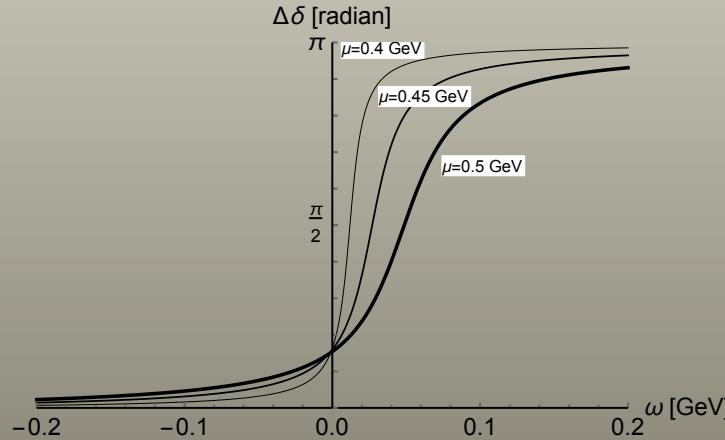


3. Case of single heavy quark

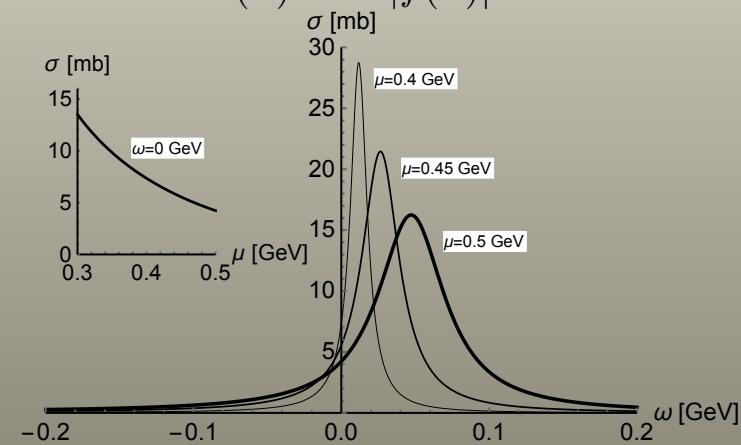


S.Y., arXiv:1608.06450 [hep-ph]

Phase shift: $\Delta\delta(\omega) = \pi \int_{-\Lambda}^{\omega} \rho_1(\omega') d\omega'$



Amplitude: $f(\omega) = e^{i\Delta\delta(\omega)} \sin\Delta\delta(\omega)/k$
 Cross section: $\sigma(\omega) = 4\pi|f(\omega)|^2$



Comparable (strongly correlated system)

Mean free path: $\tau \simeq (\sigma n_q / N_f)^{-1}$

$\tau \simeq 1.3 - 0.91$ fm for $\mu = 0.3 - 0.5$ GeV

Mean distance:
 $\ell \simeq n_q^{-1/3} = 0.96 - 0.58$ fm

Conclusion of Part 1

① We study the Kondo effect of $\bar{D}s/\bar{D}s^*$ meson

$\bar{D}s/\bar{D}s^*$ meson in nuclear matter

\times HQS interaction

= “Kondo resonance”

nucleon in the ground state.

Future works:

1. Application to *realistic* $\bar{D}s/\bar{D}s^*$ meson-nucleon interaction.
2. Application to other heavy hadrons.
3. Observables and reactions for experiments.
4. etc.

Conclusion of Part 2

- ① We study Kondo effect by color exchange for charm quark in quark matter.
- ② The color-current interaction is considered.
- ③ It leads to a nontrivial ground state with mixing between light quark and heavy quark (“Kondo phase”).

Future prospects:

1. Realization in QCD phase diagram.
2. Observables in experiments.
3. Comparison to condensed matter physics. etc.

Related references

HQS doublet/singlet in exotic hadrons and nuclei

S.Y., K.Sudoh, Y.Yamaguchi, S.Ohkoda, A.Hosaka, T.Hyodo, Phys. Lett. B727, 185 (2013)
Y.Yamaguchi, S.Ohkoda, T.Hyodo, A.Hosaka, S.Y., Phys. Rev. D91, 034034 (2015)

$\bar{D}^{(*)}N$, $\bar{D}^{(*)}NN$ hadronic molecules

S.Y., K.Sudoh, Phys. Rev. D80, 034008 (2009)
Y.Yamaguchi, S.Ohkoda, S.Y., A.Hosaka, Phys. Rev. D84, 014032 (2011)
Y.Yamaguchi, S.Ohkoda, S.Y., A.Hosaka, Phys. Rev. D85, 054003 (2013)
Y.Yamaguchi, S.Y., A.Hosaka, Nucl. Phys. A927, 110 (2014)

$\bar{D}^{(*)}$ in nuclear matter and Kondo effects

S.Y., K.Sudoh, Phys. Rev. C87, 015202 (2013)
S.Y., K.Sudoh, Phys. Rev. C88, 015201 (2013)

NLO in $1/m_Q$ expansion for $\bar{D}^{(*)}$ in nuclear matter

S.Y., K.Sudoh, Phys. Rev. C89, 015201 (2014)

$D^{(*)}N$ hadronic molecules

Y.Yamaguchi, S.Ohkoda, S.Y., A.Hosaka, Phys. Rev. D87, 074019 (2013)